Abstract: This paper describes the basics of JPEG still image compression. A video is basically a sequence of frames. When multiple frames pass in front of our eyes, we visualize video rather than still images. These frames may be stored as they are captured resulting a large file size. In order to reduce the size of captured file, compression is used. This paper is the outcome of our study of MJPEG compression. MJPEG uses still image JPEG compression. The compression process involves Discrete Cosine transform, Quantization, Entropy encoding. The purpose of this paper is to give an implementation level understanding.

Keywords: DCT, Quantization, zigzag reordering, Huffman coding.

I. INTRODUCTION

The term image compression is generally used to reduce the size of multimedia without effecting or compromising the originality of it. The reduction in size can provide a facility to store more and more data in storage like hard disk etc. With the growth of computer applications the need of storage is increase for that we such an efficient techniques due to which such need can be easily fulfilled. Image compression is an application of data compression that encodes the original image with few bits. The main purpose of image compression is to reduce the redundancy of the image and efficiently store or transmit the data. Figure 1 shows the block diagram of the JPEG image compression system. The main objective of such system is to reduce the storage capacity as much as possible, and the decoded image through which it can be similar to the original image [5].

The JPEG standard is one of the techniques that is mostly used and a part of lossy compression that based on DCT. The DCT (Discrete cosine transformation) is based on the workings of separating images into parts of various different Frequencies. During the process of quantization, where the each part of compression really occurs, the less important or unnecessary frequencies are discarded and the remaining most important or necessary frequencies are used to retrieve the image in the reconstruction process. As a result, reconstructed multimedia data is a data with distortion but later this distortion is recovered by applying some techniques.

Fig 1: Encoder & Decoder [1]
II. JPEG METHOD OF COMPRESSION

The following is the overview of JPEG encoding process in image compression using DCT describes in the following steps:

1. The image is firstly broken into 8x8, 16x16 or 32x32 blocks of pixels and do Color Space Transform (RGB to YCbCr).
2. It Works from left most corners to right most or top to bottom, the DCT can be applied to each block of image.
3. Each block is starts compressing by performing quantization process.
5. DPCM on DC component.
6. RLE on AC component.
7. Entropy Coding-Huffman or Arithmetic.

III. COLOR SPACE CONVERSION

In order to achieve good compression performance, correlation between the color components is first reduced by converting the RGB color space into a decorrelated color space. In baseline JPEG, a RGB image is first transformed into a luminance-chrominance color space [4] such as YCbCr. The advantage of converting the image into luminance-chrominance color space is that the luminance and chrominance components are very much decorrelated between each other. Moreover, the chrominance channels contain much redundant information and can easily be subsampled without sacrificing any visual quality for the reconstructed image. The transformation from RGB to YCbCr is based on the following mathematical expression:

\[
\begin{bmatrix}
Y \\
C_b \\
C_r
\end{bmatrix}
= \begin{bmatrix}
0.299000 & 0.587000 & 0.114000 \\
-0.168736 & -0.331264 & 0.500000 \\
0.500000 & -0.188688 & -0.081312
\end{bmatrix}
\begin{bmatrix}
R \\
G \\
B
\end{bmatrix}
+ \begin{bmatrix}
0 \\
128 \\
128
\end{bmatrix}
\]

The value \( Y = 0.299R + 0.587G + 0.114B \) is called the luminance. It is the value used by monochrome monitors to represent an RGB color. Physiologically, it represents the intensity of an RGB color perceived by the eye. The eye is most sensitive to the Green component then it follows the Red component and the last is the Blue component. The values \( C_b \) and \( C_r \) are called chrominance values. So we take an 8*8 image. And we convert this RGB image to YCbCr through the previous matrix. So we get the value of Luminance (Y).

<table>
<thead>
<tr>
<th>Y</th>
<th>130</th>
<th>130</th>
<th>130</th>
<th>130</th>
<th>130</th>
<th>130</th>
<th>130</th>
</tr>
</thead>
<tbody>
<tr>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
</tr>
<tr>
<td>255</td>
<td>196</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
</tr>
<tr>
<td>255</td>
<td>146</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
</tr>
<tr>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
</tr>
<tr>
<td>130</td>
<td>130</td>
<td>130</td>
<td>207</td>
<td>255</td>
<td>255</td>
<td>54</td>
<td></td>
</tr>
<tr>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>173</td>
<td>74</td>
<td></td>
</tr>
<tr>
<td>255</td>
<td>215</td>
<td>138</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
<td>130</td>
</tr>
</tbody>
</table>

IV. DISCRETE COSINE TRANSFORM

To apply the DCT, the image is divided into 8×8 blocks of pixels. If the width or height of the original image is not divisible by 8, the encoder should make it divisible. The 8×8 blocks are processed from left-to-right and from top-to-bottom [2].
The purpose of the DCT is to transform the value of pixels to the spatial frequencies. These spatial frequencies are much related to the level of detail present in an image. High spatial frequencies correspond to high levels of detail, while lower frequencies correspond to lower levels of detail. The mathematical definition of DCT is:

**Forward DCT:**

\[
F(u, v) = \frac{1}{4} C(u)C(v) \sum_{x=0}^{7} \sum_{y=0}^{7} f(x, y) \cos \left( \frac{\pi(2x+1)u}{16} \right) \cos \left( \frac{\pi(2y+1)v}{16} \right)
\]

for \( u = 0, \ldots, 7 \) and \( v = 0, \ldots, 7 \)

where \( C(k) = \begin{cases} \sqrt{2} & \text{for } k = 0 \\ 1 & \text{otherwise} \end{cases} \)

**Inverse DCT:**

\[
f(x, y) = \frac{1}{4} \sum_{u=0}^{7} \sum_{v=0}^{7} C(u)C(v)F(u, v) \cos \left( \frac{\pi(2x+1)u}{16} \right) \cos \left( \frac{\pi(2y+1)v}{16} \right)
\]

for \( x = 0, \ldots, 7 \) and \( y = 0, \ldots, 7 \)

The \( F(u, v) \) is called the DCT coefficient, and the DCT basis is:

\[
\omega_{x,y}(u, v) = \frac{C(u)C(v)}{4} \cos \left( \frac{\pi(2x+1)u}{16} \right) \cos \left( \frac{\pi(2y+1)v}{16} \right)
\]

Then we can rewrite the inverse DCT to:

\[
f(x, y) = \sum_{u=0}^{7} \sum_{v=0}^{7} F(u, v) \omega_{x,y}(u, v) \quad \text{for } x = 0, \ldots, 7 \text{ and } y = 0, \ldots, 7
\]

And \( f(x, y) \) is the matrix of values \( Y \) from the original image. Let’s take an 8x8 block of pixel values from an image:

\[
Y = \begin{bmatrix}
130 & 130 & 130 & 130 & 130 & 130 & 130 \\
130 & 130 & 130 & 130 & 130 & 130 & 130 \\
255 & 196 & 130 & 130 & 130 & 130 & 130 \\
255 & 146 & 130 & 130 & 130 & 130 & 130 \\
130 & 130 & 130 & 130 & 207 & 255 & 255 \\
130 & 130 & 130 & 130 & 130 & 173 & 74 \\
255 & 215 & 138 & 130 & 130 & 130 & 130
\end{bmatrix}
\]

The DCT can now be applied on original matrix which results in following matrix.

\[
F(u, v) = \begin{bmatrix}
1138.5 & 74.4 & 39.9 & 103.2 & -19.1 & 35.5 & -22.4 & 14.3 \\
-36 & -3.8 & 12 & -34.2 & 30.3 & -13.6 & 18.4 & -8.1 \\
-19 & 7.1 & 1.5 & -23.1 & -4.4 & -11.3 & -8.4 & -5.7 \\
-35 & -92.1 & -83.4 & 8.4 & -51.1 & -11.3 & -9.6 & 13.6 \\
-9.6 & 31 & 37.6 & -27.3 & 37.8 & -14 & 17.6 & -9.5 \\
-4.16 & 14.2 & 7.5 & 10.8 & 4.6 & 19.2 & -1.7 & 7.4 \\
78.4 & 11.2 & 6.9 & 45.8 & -14.2 & -3.1 & -5.4 & 0.7 \\
-40.3 & 14.5 & 12.2 & -38.3 & 10.9 & -12.2 & -4.3 & -8.6
\end{bmatrix}
\]
This matrix now contains 64 DCT coefficients. The upper left coefficient correlates to the low frequencies. The lower right values represent higher frequencies. As human eye is more sensitive to low frequencies, the next step of quantization will reflect this fact.

V. QUANTIZATION

The transformed 8×8 block now consists of 64 DCT coefficients. The first coefficient \( F(0, 0) \) is the DC component and the other 63 coefficients are AC component. The DC component \( F(0,0) \) is essentially the sum of the 64 pixels in the input 8×8 pixel block multiplied by the scaling factor \((1/4)C(0)C(0)=1/8\) as shown in equation 3 for \( F(u,v) \). The next step in the compression process is to quantize the transformed coefficients. Each of the 64 DCT coefficients is uniformly quantized. The 64 quantization step-size parameters for uniform quantization of the 64 DCT coefficients form an 8×8 quantization matrix. Each element in the quantization matrix is an integer between 1 and 255. Each DCT coefficient \( F(u,v) \) is divided by the corresponding quantizer step-size parameter \( Q(u,v) \) in the quantization matrix and rounded to the nearest integer as

\[
F_q(u,v) = \text{Round} \left( \frac{F(u,v)}{Q(u,v)} \right)
\]

The JPEG standard does not define any fixed quantization matrix. It is the prerogative of the user to select a quantization matrix. We have a quantization matrix for Luminance:

\[
Q (u, v) = \begin{bmatrix}
16 & 11 & 10 & 16 & 24 & 40 & 51 & 61 \\
12 & 12 & 14 & 19 & 26 & 58 & 60 & 55 \\
14 & 13 & 16 & 24 & 40 & 57 & 69 & 56 \\
14 & 17 & 22 & 29 & 51 & 87 & 80 & 62 \\
18 & 22 & 37 & 56 & 68 & 109 & 103 & 77 \\
24 & 35 & 55 & 64 & 81 & 104 & 113 & 92 \\
49 & 64 & 78 & 87 & 103 & 121 & 120 & 101 \\
72 & 92 & 95 & 98 & 112 & 100 & 103 & 99
\end{bmatrix}
\]

The resulted matrix after division is:

\[
F_q(u,v) = \begin{bmatrix}
71 & 6 & 3 & 6 & 0 & 0 & 0 & 0 \\
-3 & 0 & 0 & -1 & 1 & 0 & 0 & 0 \\
-1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
-2 & -5 & -3 & 0 & -1 & 0 & 0 & 0 \\
0 & 1 & 1 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{bmatrix}
\]

Here, zeros represent the higher frequencies that have been discarded. This results in lossy compression. Only the remaining non zero coefficients will be used to reconstruct the image.

VI. ZIGZAG REORDERING

Now the 8×8 matrix has been quantized and more than half of the DC coefficients are equal to zero.

JPEG incorporates run-length coding to take advantage of this by encoding quantized coefficients in the zigzag sequence as shown in figure below [1].
The quantized 8x8 matrix can be reordered into a 64x1 vector that will place all the non-zero entries from the matrix in the first few entries of the new vector. The string of zeros following the last non-zero entry can be eliminated as it contains unnecessary information. The zigzag reordering pattern turns the matrix into a long string of matrix coefficients, which will be shown as a row vector.

\[ V = [71, 6, -3, 1, 0, 3, 6, 0, 2, 0, -5, 0, -1, 0, 0, 1, 0, -3, 1, 1, 0, 0, 0, 0, 0, 0, \ldots] \]

All the zeros that follow the last “1” will be eliminated and “end of block (EOB)” will be added which signifies that the string is from one 8x8 Matrix. Further, run-length encoding replaces values in 64-vector by a pair (skip, value), where Skip is the number of zeros before a value, and value is the value. The special pair (0, 0) specifies the end of block.

**VII. ZERO RUN LENGTH CODING OF AC COEFFICIENT**

Now we have the quantized vector with a lot of consecutive zeroes. We can exploit this by run length coding of the consecutive zeroes. Let’s consider the 63 AC coefficients in the original 64 quantized vectors first. For example, we have:

\[ V = [71, 6, -3, 1, 0, 3, 6, 0, 2, 0, -5, 0, -1, 0, 0, 1, 0, -3, 1, 1, 0, 0, 0, 0, 0, 0, \ldots] \]

We encode for each value which is not 0, than add the number of consecutive zeroes preceding that value in front of it. The RLC (run length coding) is:

\[(0, 71); (0, 6); (0, -3); (0, -1); (1, 3) \ldots \]

EOB (End of Block) is a special coded value. If we have reached in a position in the vector from which we have till the end of the vector only zeroes, we’ll mark that position with EOB and finish the RLC of the quantized vector. Note that if the quantized vector does not finishes with zeroes (the last element is not 0), we do not add the EOB marker.

**VIII. DIFFERENCE CODING OF DC COEFFICIENTS**

Because the DC coefficient contains a lot of energy, it usually has much larger value than AC coefficients, and we can notice that there is a very close connection between the DC coefficients of adjacent blocks. So, the JPEG standard encode the difference between the DC coefficients of consecutive 8x8 blocks rather than its true value. The mathematical represent of the difference is:

\[ \text{Diff}_i = DC_i - DC_{i-1} \]

And we set DC_0 = 0. DC of the current block DC_i will be equal to DC_{i-1} + Diff_i. So, in the JPEG file, the first coefficient is actually the difference of DCs as shown in Fig. 8. Then the difference is Huffman encoded together with the encoding of AC coefficients.

**IX. HUFFMAN CODING**

In depth coverage of coding is beyond the scope of this paper. The zigzag coefficients are encoded using run-length encoding and Huffman coding. Huffman coding is based on the frequency of the symbols being encoded and not on the symbols themselves, so it allows redundancies in the symbols to be compressed. The length of each codeword is a function of its relative frequency.
frequency of occurrence. Smaller codeword represents the most common symbol. Huffman coding is also uniquely decodable, which means that the code generated from a string cannot represent something other than the original input when it is decoded [1].

X. CONCLUSION

Image compression is an extremely important part of modern computing. By having the ability to compress images to a fraction of their original size, valuable (and expensive) disk space can be saved. Further, Image compression has played an important part in the transportation of images from one computer to another becomes easier and less time consuming. The JPEG image compression algorithm provides a very effective way to compress images with minimal loss in quality. We have introduced the basic concepts of image compression and the overview of JPEG standard. It is very useful for storing pictures as visually unimportant information can be discarded. It has become the most popular image format. In this paper, the ability of the JPEG image compression to retain image quality while drastically reducing the file size is introduced through the implementation of DCT, quantization, reordering and Huffman coding.

References